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Abstract

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Reference


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Two-Dimensional Fermi Liquid with Attractive Interactions

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We realize and study an attractively interacting two-dimensional Fermi liquid. Using momentum-resolved photoemission spectroscopy, we measure the self-energy, determine the contact parameter of the short-range interaction potential, and find their dependence on the interaction strength. We successfully compare the measurements to a theoretical analysis, properly taking into account the finite temperature, harmonic trap, and the averaging over several two-dimensional gases with different peak densities.

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Atomic quantum gases have been proposed as quantum simulators to identify the microscopic origin of condensed matter phenomena, which have been pondered for decades. One such phenomenon is the Fermi liquid [1], which has been the cornerstone of the description of solids for the last 50 years. The underlying concept of this remarkable theory is that, although the basic quantum particles can be strongly interacting, there are some excitations—named Landau quasiparticles—that are essentially noninteracting. These excitations have the same quantum numbers (charge and spin) as the original particles, but their dynamical properties can be significantly different. Quasiparticle dynamics is described by a fundamental function called the self-energy, whose real and imaginary parts encode information about the quasiparticle dispersion and decay, respectively. In general, this function has a rich structure representing a variety of single-particle excitations as a function of momentum and energy. In the low-energy and low-temperature regime, the self-energy reduces to essentially two numbers, the quasiparticle effective mass and the lifetime. For interacting Fermi gases, the quasiparticle picture allows us, therefore, to summarize the effects of all the interactions in the redefinition of these two parameters, and to treat the interacting quantum system as a free-fermion gas of quasiparticles. This constitutes an immense simplification over a fully interacting quantum system and has often been the starting point to understanding more complex phenomena such as semiconductors and the transistor, superconductivity, the BCS theory, and, more recently, the giant magnetoresistance.

The initial experimental verifications of Fermi liquid theory were quite indirect and mostly based on collective mode propagation and transport measurements, for example, in simple metals, heavy-fermion materials (CeAl3, LaRu2Si2), and liquid 3He. Only in recent years, the angle-resolved photoemission spectroscopy (ARPES) technique has allowed for a direct measurement for the probability to find a single-particle excitation with a given momentum and energy—the so-called spectral function [2]. It has therefore been instrumental in providing a direct measure for the existence and properties of quasiparticles. However, the analysis of APRES spectra and a detailed comparison with the theory remains difficult in solid-state systems due to nontrivial interactions in the final state, and insufficient knowledge of the dispersion even for noninteracting particles. The clean Fermi liquid system of 3He does not easily lend itself to the equivalent of an ARPES measurement.

Experiments with cold atomic gases provide a remarkable alternative to tackle the question of interactions in quantum fluids. These systems have the advantage of combining short-range interactions with an unprecedented control of the interaction strength. They also offer control of the dimensionality of the system, and in particular have allowed the realization of interacting two-dimensional fermionic systems [3–6]. It was thus natural to develop an equivalent of the ARPES technique for cold atoms to probe the quasiparticle dynamics and the characteristics and properties of Fermi liquids [7]. However, despite successes in realizing ARPES experiments [5,8,9] and probing the formation of a gap for attractive interactions, no comparison with the properties of two-dimensional Fermi liquids has yet been made. Some aspects of Fermi liquid properties in cold gases have so far been probed only in three dimensions [10,11] by studying the magnetic susceptibility in the strongly interacting regime above \( T_c \).

Here, using momentum-resolved radiofrequency (rf) spectroscopy [5,7–9], we extract the self-energy of a two-dimensional Fermi gas with attractive interactions. We find quantitative agreement with calculations based on Fermi liquid theory. Moreover, we show that the Hartree energy term can play a dominant role in the quantitative understanding of ARPES spectra in harmonically confined Fermi gases.

We prepare a quantum degenerate Fermi gas of \(^{40}\)K atoms in the \( |F = 9/2, m_F = -9/2\rangle \) and \( |F = 9/2, m_F = -7/2\rangle \) hyperfine states in a one-dimensional optical lattice of wavelength \( \lambda = 1064 \) nm, populating a stack of approximately 40 individual two-dimensional quantum gases [3]. In the central
layers, we confine a few thousand atoms per two-dimensional gas. The radial confinement is harmonic with a trap frequency of $\omega_r = 2\pi \times 127$ Hz, and the axial trap frequency is $\omega_z = 2\pi \times 75$ kHz. After we ramp to the desired magnetic field value near the Feshbach resonance between the $| -9/2 \rangle$ and $| -7/2 \rangle$ states, we perform momentum-resolved radiofrequency spectroscopy between the $| -7/2 \rangle$ and $| F = 9/2, m_F = -5/2 \rangle \equiv | -5/2 \rangle$ states [5,9]. To this end, we apply a rf pulse of approximately $\Omega_{rf} = 47$ MHz with a Gaussian amplitude envelope with a full width at half maximum of 280 $\mu$s. After a further 100 $\mu$s, we turn off the optical lattice, switch off the magnetic field, and separate the three spin components by applying a magnetic field gradient. After letting the gas expand freely for 12 ms, we take an absorption image and average the density distribution of the state.

The result of our calculation for $1/\ln(k_F a_{2D}) = 0.35$. A free particle corresponds to a straight horizontal line. (b) Energy distribution curves at different momenta $h\mu$. The solid lines represent a fit to the data. We see a shift of the maximum toward lower energies, which indicates the effective mass of the quasiparticles. The dashed line indicates $E_0$, the position of the peak at $k = 0$. (c) and (d) Calculated intensity and energy distribution curves for the same parameters as in the experiment.

FIG. 1 (color online). Momentum-resolved photoemission signal in experiment and theory. (a) Measured signal at $1/\ln(k_F a_{2D}) = 0.35$. A free particle corresponds to a straight horizontal line. (b) Energy distribution curves at different momenta $h\mu$. The solid lines represent a fit to the data. We see a shift of the maximum toward lower energies, which indicates the effective mass of the quasiparticles. The dashed line indicates $E_0$, the position of the peak at $k = 0$. (c) and (d) Calculated intensity and energy distribution curves for the same parameters as in the experiment.

broadening of 1.5 kHz was applied to the theoretical data, which is experimentally measured for the noninteracting gas, and which corresponds to the Fourier-limited width of the rf pulse. For the interacting gas, we experimentally observe a larger width, which is not captured by theory, and which therefore possibly stems from final-state interactions.

We analyze the dispersion of the peak in Fig. 1 by means of two parameters, the $k = 0$ intercept $E_0$, and the curvature represented by an effective-mass parameter $m^*$, according to $E_{\text{max}}(k) = E_0 + b k^2/2 \left( \frac{1}{m} - \frac{1}{m^*} \right)$. In Fig. 2, we show the effective mass parameter for different values of $1/\ln(k_F a_{2D})$ at $T/T_F = 0.27$. For zero interaction, $m^*$ equals the free-particle mass to within 1% and $E_0 = -1.0(0.3)$ kHz. This data point calibrates our weak final-state interactions. Increasing the interaction strength on the attractive side of the Feshbach resonance leads to an increase of $m^*$ as the dressing of the bare fermions increases. Experimentally, $E_0$ does not show a significant variation over this range.

Our experimental results and theoretical calculations display very good agreement with each other (see Fig. 2). The thick blue line shows the theoretical $m^*/m$ for the experimental Fermi energy and temperature, and averaged over a distribution of two-dimensional gases with a...
FIG. 2 (color online). Dependence of the effective mass parameter on the interaction parameter $1/\ln(k_F a_{2D})$. The thick blue line shows the numerical calculation of the trap average and averaging over a density distribution with an rms width of 46 layers for the experimental conditions. The red dashed curve is the trap average for the central layer only. The thin green curve includes only the Hartree term in the self-energy.

Gaussian envelope of Fermi energies with a rms width of 46 layers. The dashed red line shows the result for the trap average of the center layer only, indicating that the averaging over several layers has only a very minor effect. When only the first-order Hartree term in the self-energy—a density-dependent shift without dynamical consequences—is taken into account (green curve in Fig. 2), one obtains a nonlinear dependence of the Fermi liquid properties, we vary the temperature at an approximately constant density. The dimensionless contact parameter $C$ is the trap average for the central layer only. The thin green curve agrees very well with theory.

Finally, we turn our attention to the contact parameter $C$ [22–27]. The contact is determined by the two-particle correlation function between atoms of opposite spin at short distance $g^{(2)}(|r_1 - r_1|)$, and it governs the momentum distribution of a gas at large momenta according to $n(k) \sim C/k^4$ for $k \gg k_F$. Through the universal Tan relations [22], the contact parameter provides an important link between the microscopic physics of the short-range atom-atom interactions and thermodynamic quantities. In three dimensions, the contact has been measured from photoemission spectra [25] and Bragg scattering [26], and Tan’s relations have been experimentally verified. In two dimensions, Tan’s relations have to be refined, and the spectral line shape of rf spectra receives nontrivial corrections [27].

The dimensionless contact parameter $C' = C/k_F^2$ can be measured from the high-frequency tail of the momentum-integrated single-particle spectral function [28]. In two dimensions, the spectral intensity $I_\nu(\nu')$ normalized to the intensity of the rf pulse relates to the contact by [27]

$$I_\nu(\nu') = \frac{C'}{2\pi \nu'^2} \ln^2(\frac{\tilde{E}_B}{E_B}) \ln^2(\frac{\nu'\nu}{E_B}) + \pi^2 = C' \times I(\nu').$$  \hspace{1cm} (1)

Here, $\nu' = h \nu / E_F$, and $\tilde{E}_B = \tilde{E}_{B,3D}$ is the binding energy of the most weakly bound state of atoms in the final state. Since the three-dimensional binding energy between the $|-9/2\rangle$ and $|-5/2\rangle$ states is $\tilde{E}_{B,3D} = h \times 3$ MHz [29] (in the relevant magnetic field range between 204 G and 209 G) and therefore much larger than $\hbar a_0$, the effects of quasi two—dimensional confinement on the binding energy can be neglected. Generally, final state interactions can play a significant role for the contact in two dimensions since their contribution disappears only logarithmically with increasing binding energy of the final state.

We extract the contact $C'$ from the data by dividing the momentum-integrated intensity of the spectrum by the function $I(\nu')$ and fitting the resulting constant at large $\nu'$. The inset in Fig. 4 shows an example for a typical data set. In Fig. 4, we plot the measured $C'$ as a function of $1/\ln(k_F a_{2D})$ at $T/T_F = 0.27$ (solid blue points). We compare our experimental results with the theory for the trapped

FIG. 3 (color online). Temperature dependence of the effective mass parameter. For our lowest temperature $T/T_F = 0.27$, this corresponds to an interaction strength of $1/\ln(k_F a_{2D}) = 0.35$; samples at higher temperatures contain more atoms and have a slightly larger Fermi energy, which decreases the coupling strength to $1/\ln(k_F a_{2D}) = 0.32$ at $T/T_F = 1.09$. The lines show the numerical simulation for the experimental parameters. The thick blue line is the trap average over 46 layers corresponding to the experimental conditions. The red dashed curve is the trap average for the central layer only. The thin green line includes only the Hartree term in the self-energy. The difference between Hartree only and the full self-energy changes with the number of trapped atoms, showing the intricate relation between the Hartree energy and the effective mass parameter.
gas at finite temperatures (solid blue line). The contact was calculated using the theoretical momentum-integrated spectral function and fitting a pure $1/\nu^2$ decay, as the theory does not include final-state interactions. Our calculations show that the value of $C'$ is reduced by temperature and inhomogeneity due to the transfer of spectral weight induced by the Hartree term from the $1/\nu^2$ tail to low energy.

The agreement is excellent in the regime of weak coupling. The calculation of the temperature-dependent contact at larger coupling requires further study, as the effects of the bound state become important when $E_B$ approaches $k_BT$. For comparison, we also show the zero-temperature prediction of the contact for a homogeneous system based on a quantum Monte Carlo calculation [30] (dashed gray line). In order to derive the contact from the total energy data of Ref. [30], we have used the adiabatic theorem $dE'/d[\ln(k_Fa_{2D})]=C'/\pi$, where $E'=E/E_F$. In the weak coupling regime, both the experimental results as well as our theoretical values are slightly below the zero-temperature theory. This is the expected behavior of the contact, which decreases with increasing temperature. In the strongly interacting regime, our data come closer to the zero temperature prediction, possibly because when $E_B>k_BT$ the contribution of the bound state to the contact becomes more dominant. Finally, we also show the prediction of the contact for the homogeneous Fermi liquid at zero temperature, which has been derived from the power series expansion of the total energy per particle [13] $2E'/N = 1 - 1/\ln(k_Fa_{2D}) + A/\ln(k_Fa_{2D})^2 + \ldots$ with $A=3/4-\ln(2)$.

The above results show that momentum-resolved rf spectroscopy can be employed to extract important information about a Fermi liquid, such as the self-energy, and that disentangling the dynamical part of the self-energy from the nontrivial contributions arising from the Hartree term in the trap is important. The latter could be overcome only by using confining potentials different from the usually employed harmonic potential, since our theoretical analysis shows that the Hartree contribution is independent of the strength of the harmonic potential.

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